

## Temperature, Internal Energy and Heat

Big Idea - everything is made of atoms of molecules in motion.

Temperature is the average kinetic energy of the particles (atoms and molecules) that make up stuff.

For an ideal gas,  
Boltzmann's constant  
 $k_B = 1.38 \times 10^{-23} \text{ J/K}$

$\bar{E}_k = \frac{3}{2} k_B T = \frac{3}{2} (R/N_A) T$  the average kinetic energy of the particle composing an ideal gas.

T is temperature in Kelvin  
convert from Kelvin to Celsius, subtract 273.15°  
Celsius scale is based on freezing water at 0  
Celsius and boiling water at 100°C at 1 atm =  
101.3kPa

Kelvin is also based on water for the change, so  
a change in Kelvin = change in Celsius  
but zero kelvin is when the kinetic energy of the  
particles = 0 (stop)  
absolute zero - you can't move slower than not  
moving

eg. The temperature in the classroom is 20.0°C.  
What is the

a) temperature in Kelvin

$$20.0 + 273.15 = 293.15 = 293.2\text{K}$$

a) the average kinetic energy of the air molecules?

$$\begin{aligned} E_k &= \frac{3}{2} k_B T \\ &= \left(\frac{3}{2}\right) \times (1.38 \times 10^{-23}) \times (293.15) = \\ &= 6.07 \times 10^{-21} \text{J} \end{aligned}$$

a) the average speed of the air molecules  
(assume air is N<sub>2</sub>, molecular mass of  
28g/6.02x10<sup>23</sup>)

$$\begin{aligned} E_k &= \frac{1}{2} m v^2 \quad v = \\ &= \sqrt{2 \times (6.07 \times 10^{-21}) / (0.028 / 6.02 \times 10^{23})} = \\ &= 510.8913778877074 \\ &= 511 \text{m/s} \end{aligned}$$

a) what is your favourite colour?

Green

The sum of all the molecular collisions causes air pressure.

$P = F/A$  force/area, in Pascal,  $\text{Pa} = \text{N/m}^2$

$F = \Delta p / \Delta t$  the change in momentum of the air particles produce the force

Ideal Gas Law:

$$PV = nRT$$

P is pressure, in Pa (if V in m<sup>3</sup>) or in kPa (if V in Litres)

V is Volume in m<sup>3</sup> or L

R= 8.31 J/Kmol

N/m<sup>2</sup> x m<sup>3</sup> = Nm = J

or kPa x L = J 1000N/m<sup>2</sup> x 1/1000 m<sup>3</sup> = J

n number of moles of the gas = number of molecules/avagadro's number 6.02x10<sup>23</sup> 1/mol

T is temperature in Kelvin

If a gas is compressed or expanded, it does work.

W= Fs

P=F/A

W=PA s = PΔV

W=PΔV

area under a P-V graph - for reversible heat engines - it is the area inside the P-V graph

eg. A 2.0 L cylinder of Nitrogen at 20.0°C and 1.000 atmosphere (101.3kPa) is expanded while the pressure decreases linearly to half an atmosphere to 4.0L.

a) How many moles of nitrogen are in the cylinder?

$n = PV/RT = 101.3\text{kPa} \times 2.0 \text{ L} / 8.31\text{J/Kmol} \times 293.15 = 0.083 \text{ mol}$

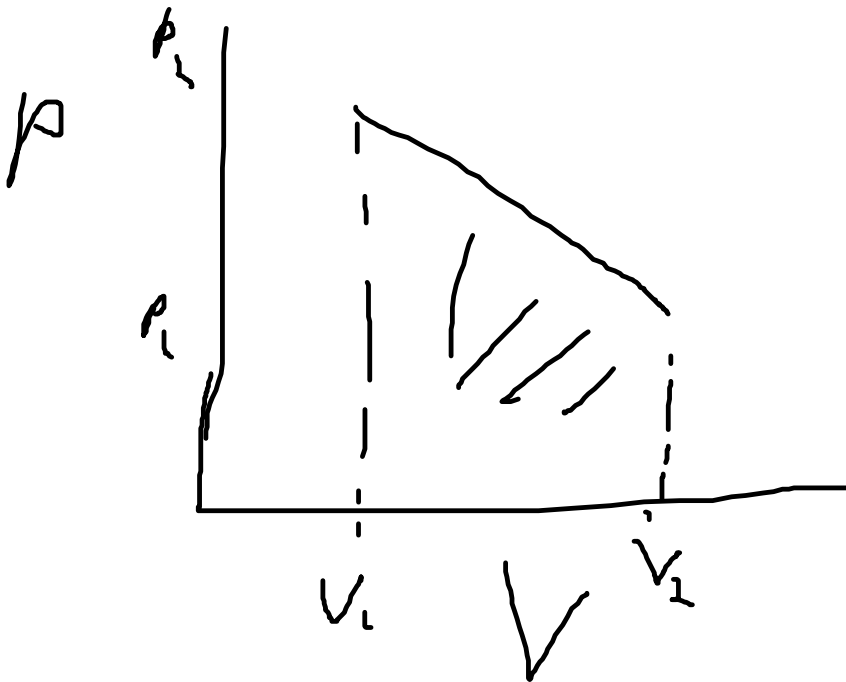
b) What is the new temperature of the gas?

T= same 20.0°C (half the pressure but double

the volume, PV)

c) How much work was done by the gas?

$W = \text{area under } P\text{-}V \text{ graph}$



$$\text{area} = \frac{1}{2} (P_1 + P_2)(V_2 - V_1) = \frac{1}{2} (101.3 + 50.65)(4.0\text{L} - 2.0\text{L}) = 152\text{J}$$

<https://phet.colorado.edu/en/simulation/legacy/gas-properties>

Homework - Play with applet

P466 - 468 problems 41, 53, 75, 77, 83, 87